# (GCF-1, 3, 4, 5, 6, 7+7A, 8+8A, 9, VCF-1,2, ACF-1,2, JCF-1)

DATE: 08.10.2023 MAXIMUM MARKS: 100 TIMING: 2 Hours

## **BUSINESS MATHEMATICS, REASONING & STATISTICS**

## 1. Ans. a

Explanation:

The most appropriate diagram to represent 5 year plan outlay of India in different economic sectors is Pie diagram

### 2. Ans. d

Explanation:

Present value = 
$$A(1+i)^{-n} = 10000 / (1+0.025)^4$$
  
=  $10000 / (1.025)^4$   
=  $10000 / (1.1038)$   
=  $Rs.9059.50$ 

Explanation:

Here A = 2000, 
$$i = \frac{6}{100 \times 12} = 0.005$$
, n = 24

Let Rs. P be the each payment.

$$\therefore \text{ Amount : A = P} \left[ \frac{(1+i)^n - 1}{i} \right] \Rightarrow 2000 = P \left[ \frac{(1+0.005)^{24} - 1}{0.005} \right] = P \left[ \frac{(1.005)^{24} - 1}{0.005} \right]$$

$$\Rightarrow P = \frac{2000 \times 0.005}{(1.005)^{24} - 1} \text{ or } P = \frac{10}{1.1272 - 1} = \frac{10}{0.1272} = \text{Rs. 78.61}$$

## 4. Ans. c

Explanation:

37, 39, ... 119  

$$l = a + (n-1)d$$
  
119 = 37 + (n-1)(2)  
 $n = 42$   
 $S_n = \frac{n}{2}(a+1) = \frac{42}{2}(37+119) = 3276$ 

#### 5. Ans. d

$$x^{y} = e^{x+y}$$

$$y \log x = x + y$$

$$y = \frac{x}{\log x - 1}$$

$$\frac{dy}{dx} = \frac{\log x - 2}{(\log x - 1)^2}$$

6. Ans. b

$$F = \sqrt{L \times P}$$

$$150^2 = 144 \times P$$

$$P = 156.25$$

7. Ans. b

Explanation:

Suppose that I am x years old and my son is y years old. Then, according to question,

$$x = 3y$$
 ...(i)

and 
$$x+5=\frac{5}{2}(y+5)$$
 ...(ii)

from (i) and (ii), 
$$3y+5=\frac{5}{2}(y+5)$$

$$\Rightarrow$$
 6y + 10 = 5y + 25

$$\Rightarrow$$
 y = 15

Substituting in (i) gives,  $x = 3 \times 15 = 45$ 

Hence, my age = 45 years.

8. Ans. a

Explanation:

A = 
$$\frac{R}{r}[(1+r)^n - 1]$$
  
=  $\frac{6000}{0.09}[(1+0.09)^8 - 1]$   
= Rs. 66170.84

9. Ans. a

Explanation:

First Time 
$$A = 3x$$

$$P = x$$

$$\therefore 3x = x \left[ 1 + \frac{r}{100} \right]^6$$

$$3 = \left[1 + \frac{\mathbf{r}}{100}\right]^6$$

Second Time

$$A = 27x$$

$$P = x$$

$$n = ?$$

$$27x = x \left[ 1 + \frac{r}{100} \right]^n$$

$$(3)^3 = \left[1 + \frac{r}{100}\right]^n$$

$$\left\{ \left[ 1 + \frac{\mathbf{r}}{100} \right]^6 \right\}^3 = \left( 1 + \frac{\mathbf{r}}{100} \right)^n$$

$$\left(1 + \frac{r}{100}\right)^{18} = \left(1 + \frac{r}{100}\right)^n \implies n = 18$$

10. Ans. b

$$f(x) = \sqrt{x + \sqrt{x + ...\infty}}$$
  

$$\Rightarrow f(x) = \sqrt{x + f(x)}$$

On squaring both sides, we get

$$[f(x)]^2 = x + f(x)$$

differentiation both sides

$$2f(x) f'(x) = 1+f'(x)$$

$$f'(x) [2f(x)-1]=1$$

$$f'(x) = \frac{1}{2f(x) - 1}$$

#### 11. Ans. a

Explanation:

Using declining balance depreciation

Declining Balance Depreciation Rate =  $1 - (Salvage Value / Cost)^{(1/Years)}$ 

Rearrange

Salvage value = Cost x (1 - Depreciation rate)^Years

Salvage value =  $10000 \times (1 - 10\%)^10 = 3,486.78$ 

#### 12. Ans. b

Explanation:

$$16000[(1 + 5\%)3 - 1] = 2522$$

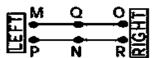
#### 13. Ans. b

Explanation:

According to question,

The sitting arrangement of M, N, O, P, Q and R would be as follows:

It is clear from the diagram that Q is facing N.



#### 14. Ans. c

Explanation:

Common Solution for the set:

In this type of linear arrangement, we find the fixed position all are facing north

Here Y is Exactly in the Middle and it is third to the left of U

1	2	3	4	5	6	7
			Υ			U

W, cannot sit at any extreme end so, T is in 1<sup>st</sup> place. W sits fifth to the right of T. W is in 6<sup>th</sup> place

1	2	3	4	5	6	7
Т			Υ		W	C

Z is not an immediate neighbor of Y. so, only one place left for Z that is 2.

1	2	3	4	5	6	7
Т	Ζ		Υ		W	U

Two people sit between Z and X, X is at  $5^{th}$  place

1	2	3	4	5	6	7
Т	Z		Υ	Χ	W	J

The last place left for V.

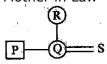
From the given information we can make the following arrangement.

1	2	3	4	5	6	7
Т	Z	V	Υ	Х	W	U

## 15. Ans. d

Explanation:

Mother in Law



## 16. Ans. d

Explanation:

Since X and Y both are the young-ones of Z. Hence either X and Y will be either sons or daughters of Z. Since Y is not the son of Z. Hence Y will be the daughter of Z.

## 17. Ans. c

Explanation:

Commodity	R	W	RW
I	110	თ	330
II	120	3	360
III	70	1	70
Total		7	760

Weighted Price Index = 
$$\frac{\Sigma RW}{\Sigma W} = \frac{760}{7} = 108.5$$

#### 18. Ans. c

Explanation:

Event A: Person aged 50 years will remain alive after 20 years

Event B: Person aged 60 years will remain alive after 20 years

$$\therefore P(A) = \frac{5}{9+5} = \frac{5}{14} \text{ and } P(B) = \frac{6}{8+6} = \frac{6}{14}$$

$$\therefore P(A \cup B) = \frac{5}{14} + \frac{6}{14} - \frac{5}{14} \times \frac{6}{14} = \frac{31}{49}$$

#### 19. Ans. a

Explanation:

Largest angle 
$$= \frac{32}{90} \times 360 = 128^{\circ}$$

Smallest angle = 
$$\frac{17}{90} \times 360 = 68^{\circ}$$

Difference =  $60^{\circ}$ 

### 20. Ans. a

Explanation:

Purchasing power of money is inversely proportional to price index number.

21. Ans. a

Explanation:

Age of applicants for life insurance and the premium of insurance-correlation positive

22. Ans. c

Explanation:

The area of a normal Curve is Unity.

23. Ans. b

Explanation:

Less than ogive & more than Ogive intersect at a point called MEDIAN or we can say second quartile.

24. Ans. b

Explanation:

The algebric sum of deviations taken from mean is zero.

Therefore  $\Sigma (X_i - \overline{X}) = 0$ 

25. Ans. a

Explanation:

Laspeyre's Price Index is based on base year Quantity.

Since Formula is 
$$L = \frac{\Sigma P_1 Q_0}{\Sigma P_0 Q_0} \times 100$$

Hence  $Q_0$  is constant.

26. Ans. b

Explanation:

Box-head is the entire upper part of the table which includes columns and subcolumn and unit of measurement.

27. Ans. a

Explanation:

Q.D<M.D.<S.D

28. Ans. b

Explanation:

If two variable are uncorrelated then regression lines are Perpendicular.

29. Ans. c

Explanation:

To check the consistency of two data which measure of dispersion will be used CV.

30. Ans. d

$$E = \left[ \left( 1 + \frac{r}{100} \right)^n - 1 \right] \times 100$$
$$= \left[ \left( 1 + \frac{6}{200} \right)^2 - 1 \right] \times 100 = 6.09\%$$

31. Ans. d

Explanation:

No. of ways = 
$$7C_4 \times 3C_2 + 7C_3 \times 3C_3$$
  
=  $105 + 35 = 140$ 

32. Ans. d

Explanation:

(a, a), (b, b), (c, c) E R

So R is a reflexive relation

But (a, b)  $\varepsilon$  R and  $(b, a) \notin R$ 

Thus, R is not a symmetric relation.

Also, (a, b),  $(b, c) \in R \Rightarrow (a, c) \notin R$ 

Hence R is not a transitive relation

33. Ans. b

Explanation:

Mean Proportion

$$= \sqrt{\frac{a-b}{a+b}} \times \frac{a^2 b^2}{a^2 - b^2}$$
$$= \frac{ab}{a+b}$$

34. Ans. c

Explanation:

Total line can be made by  $10_{c_3}$ 

and  $7_{c_2}$  lines could not be drawn because points are collinear

So Remaining 
$$\Rightarrow 10_{c_2} - 7_{c_2} + 1$$
  
 $\Rightarrow 25$ 

35. Ans. a

Explanation:

Which one of the following mean cannot be determined by graphic method.

36. Ans. c

$$x^{2} + x + 2 = 0$$

$$\propto +\beta = -1, \quad \alpha \beta = 2$$

$$(\alpha + \beta)^{2} = \alpha^{2} + \beta^{2} + 2 \quad \alpha \beta$$

$$1 = \alpha^{2} + \beta^{2} + 4$$

$$\alpha^{2} + \beta^{2} = -3$$

$$\frac{\alpha}{\beta} + \frac{\beta}{\alpha} = \frac{\alpha^2 + \beta^2}{\alpha \beta} = \frac{-3}{2}$$

37. Ans. c Explanation:

$$S \infty = \frac{a}{1-r}$$

$$a = 2, b = \frac{6}{5}$$

$$ab = \frac{12}{5}$$

38. Ans. c

Explanation:

$$\sum X^2 = n(\sigma^2 + \overline{X}^2)$$

39. Ans. d

Explanation:

Mean < Variance

40. Ans. b

Explanation:

(AUB')

$$= B - A$$

41. Ans. c

Explanation:

$$D = P \left(\frac{R}{100}\right)^2$$

$$768 = P \left(\frac{8}{100}\right)^2$$

$$P = 1,20,000$$

42. Ans. d

Explanation:

$$\mathsf{E} = \left[ \left( 1 + \frac{r}{100} \right)^n - 1 \right] \times 100$$

$$= \left[ \left( 1 + \frac{6}{200} \right)^2 - 1 \right] \times 100 = 6.09\%$$

43. Ans. b

Let the sum be Rs. x. Then,  $\left(\frac{X\times10\times7}{100\times2}\right) - \left(\frac{X\times12\times5}{100\times2}\right) = 40$ 

$$\Leftrightarrow \frac{7x}{20} - \frac{3x}{10} = 40 \Leftrightarrow x = (40x20) = 800.$$

Hence, the sum is Rs. 800.

44. Ans. b

Explanation:

$$T_5 = a + 4d = 14$$
 .....(i)

$$T_{12} = a+11d = 35 \dots (ii)$$

On solving equation (i) and (ii)

a=2

45. Ans. c Explanation:

The no. of ways = 
$${}^4P_3 \times 4!$$

$$= P_3 \times 4!$$

$$= 24 \times 24 = 576$$

46. Ans. b

Explanation:

$$-2x + 3y \ge 6$$
 Cuts on X axis (-3, 0)

and y is more than x so option (B) is Correct.

47. Ans. d

Explanation:

$$A = P \left( 1 + \frac{r}{100} \right)^n$$

$$1 = P \left( 1 + \frac{10}{100} \right)^2$$

$$P = 0.83$$

48. Ans. d

Explanation:

SI for 2 years = 
$$5,680 - 5,200 = 480$$

SI for 5 years = 
$$\frac{480}{2} \times 5$$
 = 1,200

$$P = 5,200 - 1,200 = Rs. 4,000$$

Rate = 
$$\frac{100 \times 1,200}{4,000 \times 5} = 6\%$$

49. Ans. b

$$= \log_{60}3 + \log_{60}4 + \log_{60}5$$

$$= \log_{60}60=1$$

50. Ans. c

Explanation:

1Rs.: 50P: 25P

$$4x + \frac{250 \, x}{100} + \frac{150 \, x}{100} = 120$$

$$x = 15$$

The number of coins of 25 paisa =  $6 \times 15 = 90$ 

51. Ans. d

Explanation:

Different words can be formed =  $\frac{11!}{4!4!2!}$ 

$$S = 4$$
,  $P = 2$ ,  $I = 4$ 

52. Ans. c

Explanation:

$$A = P \left( 1 + \frac{r}{100} \right)^n$$

$$\frac{25}{16}P = P(1 + \frac{r}{100})^2$$

$$\left(\frac{5}{4}\right)^2 = (1 + \frac{r}{100})^2$$

$$\frac{5}{4} = 1 + \frac{r}{100}$$

$$r = 25\%$$

53. Ans. a

Explanation:

Black Red + White Ball

$$3c_1 \times 6c_2 + 3c_2 \times 6c_1 + 3c_3 = 64$$

54. Ans. c

Explanation:

(A-B) 
$$\cup$$
 c

$$\{2, 6, 9\} \cup \{2, 6, 8\}$$

$$= \{2, 6, 8, 9\}$$

55. Ans. b

Explanation:

Revised salary = 
$$\frac{200}{110} \times 325 = 590.90$$

It means worker is in loss.

56. Ans. a

Let cost of one chair and one table are x and y respectively, then

$$5x + 3y = 350....(i)$$

$$3x + 5y = 370....(ii)$$

$$x = 40, y = 50$$

Cost of one table and two chairs is Rs. 130

## 57. Ans. a

Explanation:

No. of diagonals = 
$$n_{c_2} - n$$

Explanation:

$$n(AxB) = n(A) \times n(B)$$
  
= 5 x 3 = 15

Explanation:

$$5x + 7y - 22 = 0$$

$$6x + 2y - 22 = 0$$

$$r = \sqrt{\frac{10}{42}}$$

$$byx = \frac{-5}{7}$$

$$bxy = -\frac{2}{6}$$

$$-\frac{5}{7} = -\frac{\sqrt{\frac{10}{42}} \times \sqrt{15}}{\sigma x}$$

$$\sigma x = 2.64 6$$

#### 60. Ans. b

Explanation:

Coefficient of range = 
$$\frac{L-S}{L+S}$$

Where  $L \rightarrow$  for largest value

$$S \rightarrow$$
 for smallest value

Coefficient of range = 
$$\frac{40-10}{40+10} = \frac{30}{50} = \frac{3}{5}$$

#### 61. Ans. b

Explanation:

G.M. = 
$$(2 \times 2^2 \times 2^3 \times 2^4 \times 2^5 \times 2^6)^{1/6}$$
  
=  $2^{7/2}$ 

Revised salary = 
$$\frac{200}{110} \times 325 = 590.90$$

It means worker is in loss.

63. Ans. d

Explanation:

Regression coefficient are independent of change of origin but not scale (As per Fundamental Principle)

64. Ans. d

Explanation:

$$m = 150 \times \frac{2}{100} = 3 \quad p(more than 2) = 1 - \frac{e^{-3}3^{0}}{0!} - \frac{e^{-3}3^{1}}{1!} - \frac{e^{-3}3^{2}}{2!}$$
$$= 1 - \frac{e^{-3}3^{0}}{0!} - \frac{e^{-3}3^{1}}{1!} - \frac{e^{-3}3^{2}}{2!} = 0.58$$

65. Ans. b

Explanation:

$$\infty - \beta = \sqrt{(\infty + \beta)^2 - 4 \infty \beta}$$
$$= \sqrt{(7)^2 - 4(-9)} = \sqrt{85}$$

66. Ans. a

Explanation:

67. Ans. c

Explanation:

$$H + 2 = J$$

$$O + 2 = Q$$

$$N+2 = P$$

$$E + 2 = G$$

$$Y + 2 = A$$

Now,

$$V - 2 = T$$

$$C-2 = A$$

$$T-2 = R$$

$$I-2 = G$$

$$G-2 = E$$

$$V-2 = T$$

$$U-2 = S$$

68. Ans. c

Explanation:

MINK - M = INK

69. Ans. d

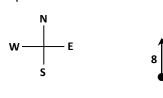
Explanation:

$$C + 2 = E + 2 = G + 2 = I$$

Then, J180P is wrong.

70. Ans. b

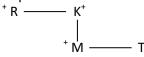
Explanation:



Correct direction SE But best option South

71. Ans. b

Explanation:



72. Ans. a

Explanation:



73. Ans. c

Explanation:

B is the son of C but C is not the mother of B means C is the father of B.

A is married to C means A is the mother of B.

F is the brother of B means F is the son of A and C.

D is daughter of A means D is daughter A and C. A is the mother and hence female. B is the son and hence male. C is the husband and hence male. D is the daughter and hence female. E is the brother and hence male. F is the son and hence male.

So, there are four males.

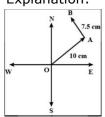
74. Ans. b

Explanation:

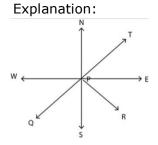
$$1, 10, 37, 118$$
 $1 \times 3 + 7 = 10$ 
 $10 \times 3 + 7 = 37$ 
 $37 \times 3 + 7 = 118$ 
 $118 \times 3 + 7 = 361$ 

75. Ans. a

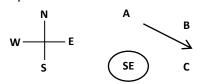
76. Ans. d Explanation:



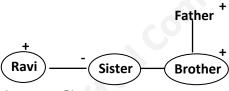
77. Ans. b



78. Ans. b Explanation:



79. Ans. c Explanation:



Answer- Sister

80. Ans. c

Explanation:

2nd = (1st + 1) : 3rd = (2nd + 2); 4th = (3rd + 3); 5th = (4th + 4).

- But 18 = 6th term not equal ? 5th + 5 = 14 + 5 = 19.
- 81. Ans. a

82. Ans. d

Explanation: Let the sides of a triangle are in 6x, 4x and 3x

Then 
$$6x + 4x + 3x = 52$$
  
  $x = 4$ 

The length of the smallest side =  $3 \times 4 = 12 \text{ cm}$ 

83. Ans. b

n = 7

Explanation:

$$\sqrt{\frac{n^2 - 1}{12}} = 2$$

$$\frac{n^2 - 1}{12} = 4$$

84. Ans. a

Explanation:

Standard Deviation is independent of change of Origin.

85. Ans. c

Explanation:

$$r = \frac{25}{6 \times 5} = \frac{25}{30} = 0.833$$

86. Ans. c

Explanation:

$$Z = 3m - 2x$$
  
 $18 = 3m - 48$   
 $66 = 3m$   
 $m = 22$ 

87. Ans. d

Explanation:

88. Ans. c

Explanation:

Intersecting point of less than ogive and more than ogive curve Median.

89. Ans. d

Explanation:

Random Variable can be All of these.

90. Ans. c

Explanation:

Skewness of normal distribution is Zero.

91. Ans. c

Explanation:

Standard Normal Variate.

92. Ans. c

Explanation:

$$A: B = 4:5] \times 7$$

$$B: C = 7:8] \times 5$$

$$A:B:C=28:35:40$$

93. Ans. b

Explanation:

$$9, G, G_2, G_3, G_4, 288$$

$$l = a r^{n-1}$$

$$288 = 9 r^5$$

$$r^5 = 2^5$$

$$r = 2$$

$$G_1 = ar = 9 \times 2 = 18$$

$$G_2 = ar^2 = 9 \times 4 = 36$$

$$G_3 = ar^3 = 9 \times 8 = 72$$

$$G_4 = ar^4 = 9 \times 16 = 144$$

94. Ans. c

Explanation:

$$\frac{d}{dx}(x^2 \log x)$$

$$= x^2 \cdot \frac{1}{x} + 2x \log x$$

$$= x (1 + 2 \log x)$$

95. Ans. a

Explanation:

Chronological classification is classification of units on the basis of time.

96. Ans. c

Explanation:

$$New Mean = \frac{\bar{x}}{\alpha} \qquad New Mean = \frac{\bar{x}}{\alpha} + 10$$

97. Ans. d

Explanation:

$$P_{01} = \sqrt{\frac{\sum P_1 q_0}{\sum P_0 q_0}} x \frac{\sum P_1 q_1}{\sum P_0 q_1} x 100 = 94.88$$

98. Ans. b

$$\frac{1}{2} \times \frac{1}{x} = \frac{1}{3} \times \frac{1}{5}$$

$$x = \frac{15}{2}$$

99. Ans. c

Explanation:

Sum of deviation from mean for any set of observation is Zero.

Therefore  $\Sigma \left( X_i - \overline{\overline{X}} \right) = 0$ 

100. Ans. b

Explanation:

Χ	Р	PX
5	1/3	5/3
6	1/4	6/4
7	5/12	35/12

$$\frac{5}{3} + \frac{6}{4} + \frac{35}{12}$$
$$\frac{20 + 18 + 35}{12} = 6.08$$

\_\_\*\*\_\_